Evidence for Dominant Phonon-Electron Scattering in Weyl Semimetal WP$_2$

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Topological semimetals have revealed a wide array of novel transport phenomena, including enormous magnetoresistance and mobilities$^{[1–5]}$. Observations of such behavior in topological systems suggest that the quantum geometry of the electronic bands is a crucial ingredient. However, nontopological semimetals such as LaAs, PtSn$_4$, and $\alpha$-WP$_2$ have revealed similarly remarkable magnetoresistances and mobilities$^{[6–8]}$, suggesting that these properties are more endemic to semimetals, in general, with some works proposing that the primary factor is near-perfect electron-hole compensation$^{[6]}$. In addition, there is often enormous variation in the temperature dependence of these properties, indicating that temperature-dependent scattering processes, as those provided by electron-phonon coupling, are important.

The transition metal dipnictide WP$_2$ is an ideal semimetal to study the role of coupling between the electron and phonon systems. The topological phase $\beta$-WP$_2$ displays the largest magnetoresistance of any topological semimetal$^{[3]}$, with hints of hydrodynamic behavior at low temperatures$^{[9]}$. In WP$_2$, the resistivity decreases while the mobility increases by 4 and 5 orders of magnitude, respectively, between room temperature and 2 K$^{[3]}$. Over the temperature range where the majority of this change occurs, the resistivity appears to be dominated by electron-phonon scattering$^{[3,10]}$. Previous computational works also suggested that electron-phonon coupling plays a large role in determining the macroscopic transport properties of WP$_2$$^{[11]}$.

An important and related consideration is the phonon-electron scattering, i.e., the scattering of phonons by electrons. Such scattering is of considerable importance when evaluating the lattice’s effect on transport properties. For example, if phonon-electron scattering rates exceed phonon-phonon rates, momentum lost to phonons may be returned to the charge carriers, leading to an enhanced conductance$^{[12–14]}$. Evidence for strong phonon-electron coupling in topological semimetals (TSM) has been primarily reported via optical spectroscopies that directly probe the system’s phonons$^{[15–18]}$. However, it is unclear what combination of factors contribute to the phonon-electron scattering and thus what its role is in the transport behavior of TSMs. To this end, we perform a combined experimental, computational, and theoretical investigation of the phonon-electron coupling in WP$_2$. Using Raman...
spectroscopy, first-principles calculations, and symmetry analysis, we provide evidence that phonon-electron scattering dominates over phonon-phonon scattering over a wide temperature range. The \textit{ab initio} calculations further elucidate the roles played by the relative phase space and phonon-electron coupling strength in the dominance of phonon-electron scattering.

II. PHONON LINEWIDTH MEASUREMENTS

We utilize Raman spectroscopy due to its sensitivity to symmetry, high-energy resolution, and the prevalence of phonon-electron coupling signatures in Raman spectra of other TSMs [15–18]. We begin by considering, in detail, the symmetry properties of WP$_2$. The orthorhombic, non-symmorphic space group $Cmc$$_2$$_1$ leads to a total of 18 phonon modes. The 15 optical modes are all Raman active, and a group theoretical analysis [19] gives the irreducible representations $5A_1$, $3A_2$, $2B_1$, and $5B_2$. In Fig. 1(a), we show the room-temperature Raman spectra of an as-grown WP$_2$ crystal surface measured in XX and X'X' polarization configurations, revealing 13 of the 15 optical modes. Additional spectra from another WP$_2$ crystal shown in the Supplemental Material [20] reveal one more mode $B_1(2)$, bringing the total number of observed modes to 14 of 15. The full polarization dependence yields the mode assignments shown in Fig. 1(a), which are consistent with previous studies [21,22] (Table 1 in Ref. [20]). In Fig. 1(b), we show our measured versus our computationally predicted mode energies. The solid diagonal line indicates ideal agreement, and the reported values all fall within 3% of this line.

We begin our search for signatures of phonon-electron coupling in the temperature dependence of the phonon energies. Typically, the phonon energy decreases as the temperature increases due to a combination of lattice expansion and anharmonic renormalization [23,24]. The temperature-dependent Raman spectra shown in Fig. 2(a) reveal behavior consistent with this result, with all observed modes shifting to lower energies as the temperature is increased from 10 to 300 K. A previous report indicated an anomalous decrease in mode energies below about 25 K [22], which was interpreted as evidence for phonon-electron coupling. In an initial run of low-temperature measurements, we observed similar behavior (see Supplemental Material [20]). However, in subsequent measurements, we found that this anomalous softening was removed by allowing more time for the WP$_2$ crystals to come to thermal equilibrium with the cryostat at each temperature.

To extract the quantitative behavior of the phonon energies and linewidths, we fit each mode with a Voigt profile. While an asymmetric line shape can be an indication of phonon-electron coupling [16,25], we did not observe this in any WP$_2$ mode. We also did not observe any electronic Raman scattering in the same spectral range as the optical phonons, which may explain the absence of any asymmetric line shapes, as a Fano line shape generally requires both a large coupling strength and large matrix element for electronic Raman scattering. In Fig. 2(b), we plot the percent change of each mode’s energy and observe that, while most of the modes display changes below 1%, the lowest-energy $A_1$ mode shifts by almost 2%. While this could be a sign of phonon-electron coupling, the temperature dependence of phonon energies contains contributions from multiple sources, so unambiguous interpretation is challenging [24]. We therefore turn to the inspection of the phonon linewidths that only contain information related to the decay paths available to the phonon mode [15,23].

The temperature-dependent linewidths of the two lowest-energy $A$$_1$ modes are plotted in Fig. 2(c). At temperatures below approximately 50 K, the $A_1(1)$ mode’s linewidth maintains a nearly constant value of 0.36 meV. Above this temperature, the linewidth grows rapidly, reaching a maximum value of approximately 0.65 meV at approximately 200 K, before slowly decreasing as it approaches room temperature. Though not as dramatic, a similar behavior is also seen in the $A_1(2)$ linewidth. This type of behavior is distinct from that predicted by optical phonon decay into acoustic phonons [26], as depicted in Fig. 2(e). In the Klemens model, an optical phonon of frequency $\omega$ is assumed to decay into two acoustic phonons of energy...
$\omega = 2\hbar$ and momentum $C^6 k$ to satisfy both energy and momentum conservation. The inclusion of higher-order processes in which an optical phonon decays into three acoustic phonons ($\omega = 3\hbar$) constitutes the extended Klemens model [23,24]. Because of the bosonic nature of phonons, the temperature dependence in both of these models is governed by the Bose-Einstein distribution function $n_B(\omega; T)$. Therefore, the linewidth predicted by this model monotonically increases with temperature, a trend that is not displayed by the $A_{1,1}$ and $A_{1,2}$ modes. We instead identify their temperature dependence as resulting from decay into electron-hole pairs near the Fermi surface [15]. Linewidths indicative of optical phonon decay into electron-hole pairs have previously been observed in the semimetals TaAs [15,16], NbAs [15], MoTe$_2$ [17], graphite [27,28], and Cd$_3$As$_2$ [18]. The model developed to describe such a behavior assumes that an optical phonon with $q = 0$ decays into an electron-hole pair via an interband transition. The decay rate therefore depends on the difference in occupation functions between the electron and hole states [29]. Since it is assumed that the initial state is below $E_F$ and therefore occupied, the model developed for graphene predicts a linewidth monotonically decreasing as the temperature is raised due to the occupancy change of the filled and empty states, accounted for by Fermi functions $n_F(\omega; T)$. We modified this account for the nearly parallel spin-orbit split bands of WP$_2$: $\Gamma(T) \propto n_F(\omega_a; T) - n_F(\omega_a + \omega_{ph}; T)$, where $\omega_{ph}$ is the energy of the optical phonon, and $\omega_a$ captures the distance between $E_F$ and the initial state of the electron [see Fig. 3(a)], and additional details in the Supplemental Material [20]. The inclusion of the $\omega_a$ term can result in a nonmonotonic temperature-dependent behavior because, at low temperatures, the empty initial state prevents the transition. As the temperature increases, the initial state becomes thermally populated and the decay processes turn on. The solid blue lines in Fig. 2(c) are the results of fitting this model to our measured linewidths, and over the entire measured temperature range, it reproduces our experimental data very well. From the fits, we find $\omega_a$ values of 24.48 and 22.64 meV for the $A_{1,1}$ and $A_{1,2}$ modes, respectively, consistent with transitions close to the Fermi level. The relatively close energies of the two $A_1$ modes are likely responsible for the similarity in $\omega_a$ values obtained for each mode.

Having identified the mechanism responsible for the anomalous behavior in the two lowest-energy $A_1$ modes, we turn to the $A_{2,2}$ mode whose energy is between the...
A$_1$(1) and A$_1$(2) modes. As can be seen in Fig. 2(c), the linewidth of this mode does not display any anomalous behavior and instead follows the dependence expected from the model of anharmonic decay. A fit to the data using the extended Klemens model, plotted as a solid red line, captures the observed trend and confirms this assessment. This observation suggests that the symmetry of the phonon mode may play a role in determining whether it decays into electron-hole pairs or other phonons, which is further supported by the lack of anomalous behavior in the B$_1$ or B$_2$ modes (see Supplemental Material [20]). However, symmetry is unlikely to be the only determining factor, as evidenced by the linewidths for the three higher-energy A$_1$ modes plotted in Fig. 2(d). Despite sharing the same symmetry, these three modes display behavior consistent with the anharmonic model of decay. Taken together, these observations indicate that both the symmetry and energy of the optical phonon are factors in determining its primary decay channels. As discussed later, the availability of phonon decay paths, the phonon-electron coupling strength, and momentum conservation also contribute.

### III. PHONON DECAY PATHS

#### A. Energy conservation

To understand the role of phonon energy, we turn to the available phase space for decay into electron-hole pairs. In Fig. 3(b), we show the calculated electronic band structure for WP$_2$ within ±1 eV of the Fermi level, which agrees with previous work [11,30]. Along the Σ (Γ → X), Δ (Γ → Y), and C (Y → X$_I$) cuts, the gaps between neighboring bands appear to be on an energy scale similar to the optical phonons. To confirm this, Fig. 3(c) shows a low-temperature weighted joint density of states (JDOS) (see the Appendix) for vertical (q = 0) transitions between states within an optical phonon energy (±70 meV) of $E_F$. Available transitions exist across the entire range, with the largest JDOS occurring between 40 and 60 meV. The A$_1$ modes that display phonon-electron dominated linewidths have energies of 22.4 and 35.8 meV, which have a comparatively smaller electronic JDOS. By contrast, the A$_1$ modes that fall in the 40–60 meV range display linewidths governed by anharmonic decay, indicating that the availability of electronic states is not the largest contributing factor to the phonon linewidths. As discussed later, we find that momentum conservation is also required to understand the difference between these A$_1$ modes.

#### B. Selection rules

Before addressing momentum conservation, it is instructive to consider the phonon symmetry via the selection rules for transitions between electronic bands. Because of lattice symmetries, there are only certain symmetry points and lines that will allow transitions by $q \approx 0$ phonons to occur. The Σ, Δ, and C cuts, which allow these transitions and intersect the Fermi surface, are shaded in Fig. 3(b). In addition to these cuts, there are other parts of the Fermi surface that exist at general k-points, not shown in Fig. 3(b), for which $q \approx 0$ transitions are allowed. The irreducible representations of the electronic bands along the high-symmetry cuts may be found from compatibility relations [31,32] as summarized in Table I. With the inclusion of

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spin-orbit coupling, all of the electronic bands belong to representations from the double space group, indicated by a bar.

The selection rules for intraband and interband transitions are found by taking the direct product of the irreducible representations for the electronic bands which, in general, produces a reducible representation and decomposing it into its irreducible components. A phonon-induced transition between these bands is symmetry allowed only for phonons that transform as irreducible representations contained in this decomposition. This case is schematically depicted in Fig. 3(a), where intraband transitions are depicted by a pink arrow and representations, while intraband transitions are shown with a blue arrow and representations. We note that while the only interband transition shown has \( q = 0 \), \( q \neq 0 \) transitions are also possible and will, in general, have different selection rules than those with \( q = 0 \). The full details concerning the decomposition of the direct products can be found in the Supplemental Material [20]; here, we summarize the main results. If we restrict the phonon decay via electronic interband and intraband transitions to points along the symmetry lines shown in Fig. 3(b), we find that phonons of \( \Gamma^{(2)} \), \( \Gamma^{(3)} \), or \( \Gamma^{(4)} \) \((A_2, B_2, \text{ or } B_1)\), respectively) symmetry can produce interband transitions, while intraband transitions can result from \( \Gamma^{(1)}(A_1) \), \( \Gamma^{(3)} \), and \( \Gamma^{(4)} \) phonons. However, when we consider transitions between general \( k \)-points or for points close to the lines of symmetry, we find that (a) there is no longer any distinction between the selection rules for interband or intraband transitions and (b) phonons of any representation may produce both types of transitions. Since the majority of the Fermi surface exists at general \( k \)-points [33], we conclude that both interband and intraband processes likely contribute to the observed linewidth behavior for the \( A_1(1) \) and \( A_1(2) \) modes. However, we note that, per these selection rules, only interband transitions with \( q \neq 0 \) are possible for the \( A_1 \) phonons. We therefore consider whether momentum conservation can be satisfied under our experimental conditions.

### 3. Momentum conservation

For interband phonon decay into electron-hole pairs, the momentum and energy conservation is trivially satisfied. As shown in Fig. 3(c), interband transitions with \( q = 0 \) exist across the entire range of optical phonon energies. Interband transitions with \( q \approx 0 \) will therefore have a very similar phase space. For intraband transitions, we explicitly estimate both the momentum provided by the photons and the momentum required for the electronic transition. Near the Fermi energy, we assume the electronic bands are approximately linear [34], with a slope given by the experimentally measured Fermi velocities [9]. The momentum obtained thus depends on the specific electron or hole pocket under consideration (see Supplemental Material [20] for details of the calculation), but for the \( A_1(1) \) and \( A_1(2) \) phonons, we find \( q \approx 8.57 \times 10^7 \) m\(^{-1}\) and \( q \approx 1.37 \times 10^8 \) m\(^{-1}\), respectively. In the backscattering configuration, the transferred momentum is found from the relation \( q \leq 4\pi n_i(\lambda) / \lambda \), where \( n_i(\lambda) \) is the wavelength-dependent index of refraction for the \( i \)th crystal direction and \( \lambda \) is the wavelength of the optical excitation. We use the calculated index of refraction (see Supplemental Material [20]) and find \( q \leq 9.68 \times 10^7 \) m\(^{-1}\). We therefore see that the momentum provided by the laser is enough to produce \( A_1(1) \) phonons capable of intraband transitions. However, it falls short for the \( A_1(2) \) phonon, which suggests that while both interband and intraband processes may be available for the \( A_1(1) \) phonon, only interband processes are available for the \( A_1(2) \) phonon. The lower availability of decay paths for...
the $A_1(2)$ mode may thus help explain why, despite having similar coupling strengths, the linewidth of the $A_1(1)$ mode appears to be more strongly influenced by the phonon-electron decay processes. Regardless, it is clear that the momentum necessary for an intraband transition by the higher-energy $A_1$ modes, which we estimate would have a minimum value of $q \approx 1.71 \times 10^8$ m$^{-1}$, cannot be provided by our laser, and thus only interband transitions may contribute to the phonon-electron component of their linewidths.

D. Phonon-electron coupling

The presence of $A_2$, $B_1$, and $B_2$ symmetries in the selection rules, combined with the lack of anomalous behavior in the linewidths for phonons of these symmetries (see Supplemental Material [20]), suggests that the phonon-electron coupling strength needs to be considered. Figure 4(a) presents the calculated phonon dispersion for WP$_2$, with the phonon-electron matrix element shown on each mode. Overall, the acoustic branches display greater coupling, while the optical modes have considerable coupling along the $\Delta$ and $T$ to $Y$ to $Z$ cuts, corresponding to phonon wave vectors that connect separate parts of the Fermi surface [15]. In Fig. 4(b), we show a close-up of the optical phonon dispersion along the $\Sigma$ and $\Delta$ cuts (for mode-resolved plots of these same data, see Supplemental Material [20]). For $q = 0$, the phonon-electron coupling strength for all modes is very weak, with most modes displaying a $|g|$ (see Appendix) on the order of 0.1 meV. This comparatively weak coupling suggests that interband transitions with $q = 0$ do not represent a significant source of phonon-electron scattering. For finite $q$, we see that for the $A_1(1)$ and $A_1(2)$ modes, the coupling strength increases by an order of magnitude, while for the higher-energy modes, the increase in coupling strength is not as dramatic. Despite showing similar increases in coupling strength, the $A_2(1)$ and $B_2(1)$ modes do not display a clear phonon-electron contribution to their linewidths, which suggests that for modes of these symmetries, the connection between higher phonon-electron coupling and linewidth behavior is less clear. We explicitly confirm this result by calculating the phonon-electron linewidth contribution at ambient temperatures. In the Supplemental Material [20], we show that the $A_1(1)$ and $A_1(2)$ modes possess significantly larger phonon-electron linewidth contributions compared to the other phonon modes. Overall, we find these trends in the coupling strength to be consistent with our measurements and interpretation of the phonon linewidths.

IV DISCUSSION

The calculated phonon dispersions may also explain why phonon-electron decay dominates over phonon-phonon decay. As shown in Fig. 4(a), there is no energy separation between the acoustic branches and the lowest-energy optical modes. These lower-energy optical modes involve large displacements of the heavy W atoms compared to the higher-energy modes, which are the source of scattering over phonon-phonon scattering, momentum provided to the phonons by electron-phonon scattering, which might otherwise be lost, may be returned to the electrons and lead to an enhanced conductivity. We note that these arguments are similar to those made for understanding the phonon drag effect [12], yet further studies are needed to confirm its existence and its influence on the overall transport properties.

Finally, we comment on the role that the topological features of $\beta$-WP$_2$’s electronic structure may play in the phonon-electron decay mechanism we report on. In $\beta$-WP$_2$, the Weyl nodes are located hundreds of meV below the Fermi surface [30,34]. The impact of these nodes on the transport properties of bulk WP$_2$, which are typically sensitive to the Fermi surface, is therefore questionable. For the particular phonon-electron decay mechanism discussed here, the nodes themselves do not seem to play any role in facilitating the effect since the optical phonon...
energies are an order of magnitude smaller than the depth of the Weyl nodes. We do note, though, that the spin-orbit coupling giving rise to the Weyl nodes also produces the band splitting that enables interband phonon decay paths [30]. Further evidence that this effect is not related to the topological nature of $\beta$-WP$_2$ may be found in another recent study of the phonon dynamics of $\alpha$-WP$_2$, which displayed nearly identical linewidth behavior, despite $\alpha$-WP$_2$ being topologically trivial [22]. While the topological nature of the material may not play a direct role in the phonon-electron behavior discussed here, the features of electronic bands in topological materials may provide the proper conditions for such behavior to occur. If crossed and linearly dispersing bands are found near the Fermi energy, then interband optical phonon decay may occur for phonons of arbitrary energy. As noted earlier, similar linewidth behavior has indeed been reported for TaAs and NbAs [15,16], two prototypical Weyl semimetals with Weyl nodes near their Fermi surfaces. In addition, the heavy atoms with large spin-orbit coupling found in many topological materials also lead to a reduction in the bandwidth of the acoustic phonons, limiting the available phase space for phonon-phonon scattering as discussed above. We thus conclude that while the effects we observed here could be possible in a semimetallic system regardless of its topological nature, the unique features of topological semimetals may provide a canvas well suited for their expression.

V CONCLUSIONS

By examining the temperature dependence of the optical phonon linewidths of WP$_2$, we identified electron-hole decay as the primary path for the lowest-energy $A_2$ optical phonon modes over a broad temperature range. Through the use of group theory, we further identified that both interband and intraband processes with finite momentum may contribute to this behavior. Combined with first-principles calculations, we also explained the importance of the phonon-electron coupling strength and the relative availability of phonon-phonon decay paths. This improved understanding of the phonon-induced intraband and interband scattering is valuable in a material where electron-phonon coupling has been suggested to play a vital role in its macroscopic transport properties. We anticipate that these results could be beneficial to understanding similar phonon behavior that has recently been observed in other Weyl semimetals [15,17]. In addition, the much larger phonon-electron coupling strengths calculated for the acoustic modes suggest they may display similar behavior and primarily scatter off of charge carriers at low temperatures, potentially leading to enhancements of the conductivity [12]. Confirmation of such behavior will require future investigations with probes capable of accessing the acoustic modes such as, e.g., resonant inelastic x-ray spectroscopy, neutron scattering, or Brillouin scattering.

Overall, we note that while the results we present here support the conclusion that phonons play a significant role in the transport properties of WP$_2$, more work will be required to understand the more general role of phonon-electron coupling in the dynamics of topological semimetals at large.

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G. B. O. and V. M. P. performed the primary measurements, analyzed the data, and provided the plots. G. B. O. performed the group theory analysis. Y. W., C. A. C. G., and P. N. performed the first-principles calculations. J. G. and C. F. prepared the single crystal samples. G. B. O. and K. S. B. wrote the manuscript, with contributions from other authors. P. N. and K. S. B. jointly conceived the project and ideas presented.

APPENDIX: METHODS

1. Experimental details

Raman spectra were collected in the backscattering configuration using a custom-built setup [36]. The 532-nm light from a frequency-doubled Nd:YAG laser was focused by a 100X long-working distance objective to a spot size of approximately 2 $\mu$m in a Montana Instruments cryostation, which enabled access to temperatures from 300 to 10 K. An incident power of less than 250 $\mu$W was
used to achieve satisfactory signal-to-noise ratios, with minimal laser-induced heating, which was checked using the Stokes to anti-Stokes ratio at all temperatures where the anti-Stokes signal was measurable (≥100 K). Polarization dependence was performed by the rotation of a double Fresnel rhomb, which acts as a broadband half-waveplate (see Supplemental Material [20]). Any spectra presented have been averaged, their background dark counts have been subtracted, and cosmic rays have been removed from them [37].

Fitting of the phonon features in our data was accomplished by a Levenburg-Marquardt least-squares fitting algorithm. Phonons were fit using a Voigt profile, whereby a Lorentzian representing the intrinsic phonon response is convoluted with a Gaussian to account for the instrument-induced broadening. A Gaussian linewidth of 0.217 meV (1.75 cm⁻¹), determined from fitting of the Rayleigh line, was used for the fitting. The average energy resolution of our system was 0.137 meV (1.1 cm⁻¹). Changes in phonon energies or linewidths smaller than the resolution of our system were able to be resolved, provided that the linewidth of the mode was broad enough such that the spectral feature was spread over many individual pixels.

2. Computational details

Calculations were performed using the ab initio package QUANTUM ESPRESSO [38,39] to evaluate electronic band structure, phonon dispersion, and electron-phonon interactions, combining density functional theory (DFT) and density functional perturbation theory (DFPT). Fully relativistic optimized norm-conserving Vanderbilt (ONCV) pseudopotentials [40] for the PBE exchange-correlation functional [41] were used for both Vanderbilt (ONCV) pseudopotentials for the PBE (DFPT). Fully relativistic optimized norm-conserving theory (DFT) and density functional perturbation theory k-point resolution of our system was 0.137 meV (0.217 meV − 1.75 cm⁻¹), determined from fitting of the Rayleigh line, was used for the fitting. The average energy resolution of our system was 0.137 meV (1.1 cm⁻¹). Changes in phonon energies or linewidths smaller than the resolution of our system were able to be resolved, provided that the linewidth of the mode was broad enough such that the spectral feature was spread over many individual pixels.

\[ g_{mn,v}(\mathbf{k}, \mathbf{q}) = \langle \psi_{mn}^\dagger | \partial_{\mathbf{q}} V | \psi_{mn} \rangle, \]

with \( \psi_{mn} \) being the electronic wave function and \( \partial_{\mathbf{q}} V \) the derivative of the self-consistent potential associated with a phonon \( \omega_{\mathbf{q}} \).

For the weighted JDOS and refractive index evaluations, separate DFT calculations were carried out using the implementation in Joint Density Functional Theory software JDFTx [45]. Fully relativistic ultrasoft pseudopotentials [46,47] for the PBEsol exchange-correlation functional [48] were used, as well as a uniform 6 × 6 × 8 k grid for the 6-atom standard primitive unit cell, an energy cutoff of 28 Hartrees, Fermi-Dirac smearing with a 0.01-Hartree width, and a 3 × 3 × 2 phonon supercell. Maximally localized Wannier functions [43,44] were similarly obtained to interpolate quantities for Monte Carlo Brillouin zone integration on finer k and q meshes [49]. Each transition contributing to the JDOS at that transition energy is weighted by the factor \( n_{\mathbf{F}}(E_{\mathbf{k},m}, T) - n_{\mathbf{F}}(E_{\mathbf{k},m}, T) \), where \( n_{\mathbf{F}}(E, T) \) is the Fermi-Dirac distribution function, and the transition occurs between energies \( E_{\mathbf{k},n} \) and \( E_{\mathbf{k},m} \) at the momentum \( \mathbf{k} \) for two bands indexed by \( n \) and \( m \). The results presented in Fig. 3(c) are for \( T = 4 \) K, with transitions restricted to be between states within ±70 meV of the Fermi level. The refractive index calculations are discussed in the Supplemental Material [20].


